15-251: Great Theoretical Ideas In Computer Science

Recitation 4

O, I Think I Understand Asymptotics Now

Let f,g,h be functions from $\mathbb N$ to $\mathbb N$. Prove or disprove the following:

- (a) If $f \in \mathcal{O}(g)$ and $g \in \mathcal{O}(h)$, then $f \in \mathcal{O}(h)$
- (b) If $f \in \mathcal{O}(g)$, then $g \in \mathcal{O}(f)$
- (c) For all $k \in \mathbb{R}^+$, $\log(n) \in \mathcal{O}(n^k)$.

Odd-Paz

State and prove a divide-and-conquer procedure for proportional cake cutting between any number of players. (The Even-Paz algorithm as described in lecture is an excellent starting point.)