## |5-25 I <br> Great Ideas in Theoretical Computer Science

## Lecture I.5:

On proofs + How to succeed in 251

Proof. Define $f_{i j}$ as in (5). As $f$ is symmetric, we only need to consider $f_{12}$.
$\mathbf{E}\left[f_{12}^{2}\right]=\mathbf{E}_{x_{3} \ldots x_{n}}\left[\frac{1}{4} \cdot\left(f_{12}^{2}\left(00 x_{3} \ldots x_{n}\right)+f_{12}^{2}\left(01 x_{3} \ldots x_{n}\right)+f_{12}^{2}\left(10 x_{3} \ldots x_{n}\right)+f_{12}^{2}\left(11 x_{3} \ldots x_{n}\right)\right)\right]$
$=\frac{1}{4} \mathbf{E}_{x_{3} \ldots x_{n}}\left[\left(f\left(00 x_{3} \ldots x_{n}\right)-f\left(11 x_{3} \ldots x_{n}\right)\right)^{2}+\left(f\left(11 x_{3} \ldots x_{n}\right)-f\left(00 x_{3} \ldots x_{n}\right)\right)^{2}\right]$
$\geq \frac{1}{2}\left(\binom{n-2}{r_{0}-1} \cdot 2^{-(n-2)} \cdot 4+\binom{n-2}{n-r_{1}-1} \cdot 2^{-(n-2)} \cdot 4\right)$
$=8 \cdot\left(\frac{\left(n-r_{0}+1\right)\left(n-r_{0}\right)}{n(n-1)} \cdot\binom{n}{r_{0}-1}+\frac{\left(n-r_{1}+1\right)\left(n-r_{1}\right)}{n(n-1)} \cdot\binom{n}{r_{1}-1}\right) 2^{-n}$.
Inequality (6) follows by applying Lemma 2.2.
In order to establish inequality (7), we show a lower bound on the principal Fourier coefficient of $f$ :

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\widehat{f}(\emptyset) \geq 1-2\left(\sum_{s<r_{0}}\binom{n}{s}+\sum_{s>n-r_{1}}\binom{n}{s}\right) 2^{-n}
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which implies that

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\widehat{f}(\emptyset)^{2} \geq 1-4 \cdot\left(\sum_{s<r_{0}}\binom{n}{s}+\sum_{s<r_{1}}\binom{n}{s}\right) 2^{-n}
$$



August 30th, 2017

## Piazza poll

What is your favorite TV show?

- Game of Thrones
- Breaking Bad
- Seinfeld
- Friends
- The Wire
- Sherlock
- The Sopranos
- Arrested Development
- Sesame Street
- None of the above
- I don't watch TV!



## PART I

On proofs

Proof. Define $f_{i j}$ as in (5). As $f$ is symmetric, we only need to consider $f_{12}$.

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## I. What is a proof?

2. How do you find a proof?
3. How do you write a proof ?

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## I. What is a proof ?

## 2. How do you find a proof ?

3. How do you write a proof?

## Is this a legit proof?

## Proposition:

Start with any number.
If the number is even, divide it by 2. If it is odd, multiply it by 3 and add $I$.
If you repeat this process, it will lead you to $4,2, I$.

## Proof:

Many people have tried this, and no one came up with a counter-example.

## Is this a legit proof?

## Pmopocitiom Collatz Conjecture:

Start with any number.
If the number is even, divide it by 2. If it is odd, multiply it by 3 and add $I$. If you repeat this process, it will lead you to 4,2, I.

## Proof:

Many people have tried this, and no one came up with a counter-example.

## Is this a legit proof?

## Proposition:

$313\left(x^{3}+y^{3}\right)=z^{3} \quad$ has no solution for $x, y, z \in \mathbb{Z}^{+}$.

## Proof:

Using a computer, we were able to verify that there is no solution for numbers with < 500 digits.

## Is this a legit proof?


$313\left(x^{3}+y^{3}\right)=z^{3} \quad$ has no solution for $x, y, z \in \mathbb{Z}^{+}$.
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## Is this a legit proof?

## Proposition:

Given a solid ball in 3 dimensional space, there is no way to decompose it into a finite number of disjoint subsets, which can be put together to form two identical copies of the original ball.


## Proof:

Obvious.

## Is this a legit proof?

## Banach-Tarski Theorem:

Given a solid ball in 3 dimensional space, there is a way to decompose it into a finite number of disjoint subsets, which can be put together to form two identical copies of the original ball.


## Proof:

Uses group theory... The pieces are such weird scatterings of points that they have no meaningful "volume"...

## Is this a legit proof?

## Proposition: <br> I + I = 2

## Proof:

This is obvious?

## Is this a legit proof?

## Proposition: <br> $$
1+1=2
$$

## Proof:

This is obvious!

## The story of 4 color theorem

## 1852 Conjecture:

Any 2-d map of regions can be colored with 4 colors so that no adjacent regions get the same color.


## The story of 4 color theorem

1879: Proved by Kempe in American Journal of Mathematics (was widely acclaimed)

1880: Alternate proof by Tait in Trans. Roy. Soc. Edinburgh
1890: Heawood finds a bug in Kempe's proof
I 89 I: Petersen finds a bug in Tait's proof
1969: Heesch showed the theorem could in principle be reduced to checking a large number of cases.

1976: Appel and Haken wrote a massive amount of code to compute and then check 1936 cases.
(I200 hours of computer time)


## The story of 4 color theorem

Much controversy at the time. Is this a proof?
What do you think?

Arguments against:

- no human could ever hand-check the cases
- maybe there is a bug in the code
- maybe there is a bug in the compiler
- maybe there is a bug in the hardware
- no "insight" is derived

1997: Simpler computer proof by Robertson, Sanders, Seymour, Thomas

## What is a mathematical proof?



A mathematical proof of a proposition is
a chain of logical deductions starting from a set of axioms and leading to the proposition.
propositions accepted to be true
a statement that is true or false

## Euclidian geometry

## 5 AXIOMS


I. Any two points can be joined by exactly one line segment.
2. Any line segment can be extended into one line.
3. Given any point $P$ and length $r$, there is a circle of radius $r$ and center $P$.
4. Any two right angles are congruent.
5. If a line $L$ intersects two lines $M$ and $N$, and if the interior angles on one side of $L$ add up to less than two right angles, then $M$ and $N$ intersect on that side of $L$.

## Euclidian geometry

## Triangle Angle Sum Theorem



Pythagorean Theorem

$a^{2}+b^{2}=c^{2}$

Thales' Theorem


## Euclidian geometry

## Pythagorean Theorem



Proof:


$$
\begin{aligned}
c^{2} & =(a+b)^{2}-2 a b \\
& =a^{2}+b^{2}
\end{aligned}
$$

Looks legit.

## Proof that square-root(2) is irrational

I. Suppose $\sqrt{2}$ is rational.

Then we can find $a, b \in \mathbb{N}$ such that $\sqrt{2}=a / b$.
2. If $\sqrt{2}=a / b$ then $\sqrt{2}=r / s$,
where $r$ and $s$ are not both even.
3. If $\sqrt{2}=r / s$ then $2=r^{2} / s^{2}$.
4. If $2=r^{2} / s^{2}$ then $2 s^{2}=r^{2}$.
5. If $2 s^{2}=r^{2}$ then $r^{2}$ is even, which means $r$ is even.
6. If $r$ is even, $r=2 t$ for some $t \in \mathbb{N}$.
7. If $2 s^{2}=r^{2}$ and $r=2 t$ then $2 s^{2}=4 t^{2}$ and so $s^{2}=2 t^{2}$.
8. If $s^{2}=2 t^{2}$ then $s^{2}$ is even, and so $s$ is even.

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9. Contradiction is reached.

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9. Contradiction is reached.

## Proof that square-root(2) is irrational

5a. $r^{2}$ is even. Suppose $r$ is odd.
5b. So there is a number $t$ such that $r=2 t+1$.
5c. So $r^{2}=(2 t+1)^{2}=4 t^{2}+4 t+1$.
5d. $4 t^{2}+4 t+1=2\left(2 t^{2}+2 t\right)+1$, which is odd.
5e. So $r^{2}$ is odd.
$5 f$. Contradiction is reached.

Odd number means not a multiple of 2 .
Is every number a multiple of 2 or one more than a multiple of 2 ?

## Proof that square-root(2) is irrational

5bl. Call a number $r$ good if $r=2 t$ or $r=2 t+1$ for some $t$.

$$
\begin{aligned}
& \text { If } r=2 t, r+1=2 t+1 \\
& \text { If } r=2 t+1, r+1=2 t+2=2(t+1)
\end{aligned}
$$

Either way, $r+1$ is also good.
5b2. 1 is good since $1=0+1=(0 \cdot 2)+1$.
5b3. Applying 5bl repeatedly, $2,3,4, \ldots$ are all good.

## Proof that square-root(2) is irrational

## Axiom of induction:

Suppose for every positive integer $n$, there is a statement $S(n)$.

If $S(1)$ is true, and $S(n) \Longrightarrow S(n+1)$ for any $n$, then $S(n)$ is true for every $n$.

Can every mathematical theorem be derived from a set of agreed upon axioms?

## Formalizing math proofs

## Principia Mathematica Volume 2



Russell


Whitehead

```
86
```



```
    Dem.
        \vdash.*110.631.*51/211/22.J
```




```
*110.64. 卜. }0+\mp@subsup{+}{\textrm{e}}{0}0=0\mathrm{ [*110.62]
*110.641. F. 1 + 
*110\cdot642. 卜. 2 + }0=0+\mp@subsup{+}{\textrm{e}}{2}2=2 [**110:51\cdot61.*101\cdot31] 
*110.643. 卜. }1+\mp@subsup{+}{\textrm{e}}{}\textrm{l}=
    Dem.
        ト.*110.632.*101-21/28.)
```



```
    [*54:3] =2.วト.Prop
    The above proposition is occasionally useful. It is used at least three
    times, in *113*66 and *120\cdot123*472.
```

Writing a proof like this
is like writing a computer program in machine language．

## LOHIEONIX



## AN EPIC SEARCH FOR TRUTH

## APOSTOLOS DOXIADIS nun OHRISTOS H. PAPADIMITRIIOU

 art by ALEGOS PAPADATOS and ANNIE DI dONNA
## Formalizing math proofs

It became generally agreed that you could rigorously formalize mathematical proofs.

But nobody wants to.
(by hand, at least)

# Interesting consequence: 

Proofs can be verified mechanically.

## One last story



Lord Wacker von Wackenfels
(1550-1619)

## Kepler Conjecture

16 I I: Kepler as a New Year's present (!) for his patron,
 Lord Wacker von Wackenfels, wrote a paper with the following conjecture.

The densest way to pack oranges is like this:


## Kepler Conjecture

## 16 II: Kepler as a New Year's present (!) for his patron,

 Lord Wacker von Wackenfels, wrote a paper with the following conjecture.

The densest way to pack spheres is like this:


## Kepler Conjecture

2005: Pittsburgher Tom Hales submits a 120 page proof in Annals of Mathematics.

Plus code to solve 100,000 distinct optimization problems, taking 2000 hours computer time.


Annals recruited a team of 20 refs. They worked for 4 years. Some quit. Some retired. One died. In the end, they gave up.

They said they were " $99 \%$ sure" it was a proof.

## Kepler Conjecture



Hales: "I will code up a completely formal axiomatic deductive proof, checkable by a computer."

2004-2014: Open source "Project Flyspeck":
2015: Hales and 21 collaborators publish "A formal proof of the Kepler conjecture".

## Formally proved theorems

Fundamental Theorem of Calculus (Harrison)
Fundamental Theorem of Algebra (Milewski)
Prime Number Theorem (Avigad @ CMU, et al.)
Gödel's Incompleteness Theorem (Shankar)
Jordan Curve Theorem (Hales)
Brouwer Fixed Point Theorem (Harrison)
Four Color Theorem (Gonthier)
Feit-Thompson Theorem (Gonthier)
Kepler Conjecture (Hales++)

## Summary / Bottom Line

In math, there are agreed upon rigorous rules for deduction. Proofs are either right or wrong.

Nevertheless, what constitutes an acceptable proof is a social construction.
(But computer science can help.)

## What does this all mean for 15-25I?

A proof is an argument that can withstand all criticisms from a highly caffeinated adversary (your TA).


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## I. What is a proof ?

## 2. How do you find a proof ?

## 3. How do you write a proof?

## How do you find a proof?

## No Eureka effect



## Terence Tao

## (Fields Medalist, "MacArthur Genius", <br> ...)

I don't have any magical ability. ... When I was a kid, I had a romanticized notion of mathematics, that hard problems were solved in 'Eureka' moments of inspiration. [But] with me, it's always, 'Let's try this. That gets me part of the way, or that doesn't work. Now let's try this. Oh, there's a little shortcut here.' You work on it long enough and you happen to make progress towards a hard problem by a back door at some point. At the end, it's usually, 'Oh, l've solved the problem.'

## How do you find a proof?

## Suggestions

Make I\% progress for 100 days.
(Make 17\% progress for 6 days.)
Understand the problem.
(List what is given to you. Write down what you need to derive.
Unpack definitions.)
Figure out some meaningful special cases (e.g. $n=1, n=2$ ).
Simplify the problem.
Put yourself in the mind of the adversary. (What are the worst-case examples/scenarios?)

## How do you find a proof?

## Suggestions

Look at proofs from notes, recitations.
Give breaks, let the unconscious brain do some work.
Develop good notation.
Use paper, draw pictures.

## How do you find a proof?

## Suggestions

Try different proof techniques.

- contrapositive $P \Longrightarrow Q \Longleftrightarrow \neg Q \Longrightarrow \neg P$
- contradiction
- induction
- case analysis


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## How do you write a proof?

http://www.cs.cmu.edu/~1525I/docs/proof-checklist.pdf

## PART 2

## How to succeed in 15-25I

http://www.cs.cmu.edu/~1525 I/docs/how-to-succeed.pdf

## Understand the course structure

## 2. Course notes

I. Lecture

3. Recitation


4. Homework


## Understand the course structure

I. Lecture

- provides background, motivation, insights, high-level picture.
- does not provide all the details.
- focus in lecture. take notes.


## Understand the course structure

## 2. Course notes

- does not provide background and motivation.
- provides the details at the level you need to know them.
- fully understanding concepts and definitions is crucial!!


## Understand the course structure

## 3. Recitation

- basically a small group review session.
- you'll be assigned a 50-minute time slot.
- you'll choose a spiciness level.

- come prepared.


## Understand the course structure

## 4. Homework

- engagement with the material $->$ real learning


## Understand the course structure

## 4. Homework

4 types of questions: SOLO, GROUP, OPEN COLLABORATION, PROGRAMMING

SOLO - work by yourself
GROUP - work in groups of 3 or 4
OPEN - work with anyone you would like from class
PROG - same rules as SOLO. submit to Autolab.

## Understand the course structure

## 4. Homework

Homework comes out Thu night and contains:

SOLO + PROG problems from current week
$+$
GROUP + OPEN problems from previous week

## Understand the course structure

## 4. Homework

## Homework writing sessions:

Wednesdays 6:30pm to 7:50pm at DH 23I5
Write the solutions to a random subset of the problems.
Practice writing the solutions beforehand!!!
Style matters!!!
You get $20 \%$ of the credit for the question if you write:

- nothing
- "I don't know", or
- "WTF!"


## Understand the course structure

## 4. Homework

## Homework Grading:

## Step 1:

TAs grade and give back the hw in recitation.
You will know who graded which question.

## Step 2:

If

- you think there has been a mistake in grading
- you don't understand why you lost points
email the TA who graded the question.
(attach a picture of your write-up)


## Understand the course structure

## 4. Homework

## Homework Resubmission:

Learn from your mistakes $->$ more points.

Submit electronically (via email) a completely correct solution by $6: 30$ pm Friday ( 9 days after writing sess.)

You'll get back 25\% of the lost credit on the problem.

## Understand the course structure

## 4. Homework

## Common Mistakes:

I. Starting the hw before reviewing the notes.
2. Not practicing writing up your solution.
3. Putting quantity over quality.
4. Not learning from your mistakes.

## Know when to get help

Help us help you!

## Know when to figure things out on your own

If you can figure something out yourself, you should figure it out yourself.

## Know when to let go

If you have given it an honest effort, you have done your job.

## Find the right group

Your group is going to be one of the most important parts of the course.

## Keep at it

Stamina will play a huge role!

## ADVICE FROM PREVIOUS 15-25I STUDENTS

If you leave enough time for 25 I work, it won't be stressful, it'll just be fun. But you have to leave yourself a good amount of time.

Be proactive and don't procrastinate! Take advantage of office hours!

Go to office hours. They are helpful.
get ur shit together and don't be afraid to ask for help.

GO TO THE PROF'S OFFICE HOURS AT THE BEGINNING OF THE SEMESTER.

Read the notes and slides until you completely understand them, then understand the questions on the homework completely before trying to come up with an answer.

Understand course material before starting doing homework. Definitions are really really important for this class

Pay attention in class, go to recitation, review the material every week, and go to office hours.

Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls Pls practice writing up your proofs before the homework writing sessions. I saw a solid letter grade difference whenever I did.

Choose your group carefully; make sure that you feel
comfortable calling your group members lazy bums if necessary.

Find a good group, and expect to be spending a lot of time with them. A lot of the success or failure in the class will come from how well you can work together with your group so that during homework sessions you can all learn something. There will absolutely be problems or concepts which you don't understand as well as someone else in your group, and vice versa. That way you can teach each other, which is ideal. Also, if you get stumped, absolutely attend office hours. The TA's are generally quite helpful.

Think of it as a course that will give you a fantastic overview of CS theory - the ride will be tough, but try to focus less on the grades and more on enjoying understanding the material.

