15-251
Great Ideas in Theoretical Computer Science

Lecture 1:
Introduction to the course

Instructors

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Jan 16th, 2018

Teaching Assistants

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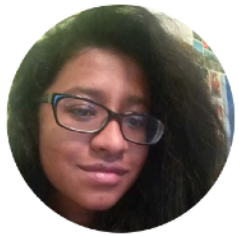

Alka Earathu
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Amulya Musipatla
amusipat

Erik Sargent
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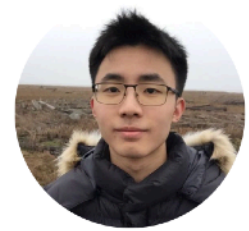

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rhogenso

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twildenh

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What is **computer science**?

What is ***theoretical* computer science**?

What is computer science?

Is it a branch of:

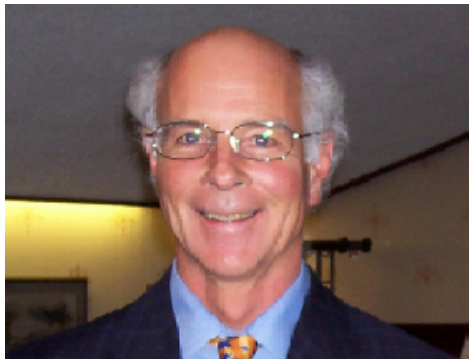
- science?
- engineering?
- math?
- philosophy?
- sports?

Motivational Quote of the Course

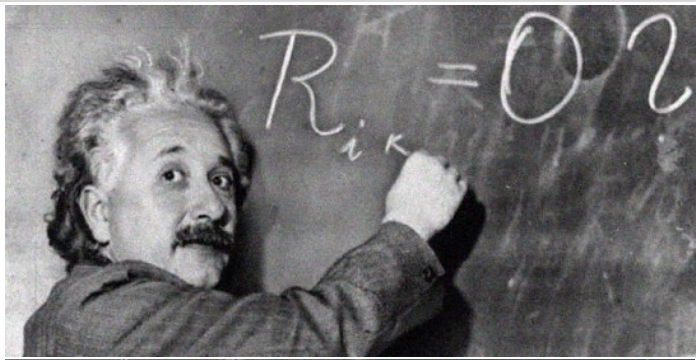
"Computer Science is no more about computers than astronomy is about telescopes."

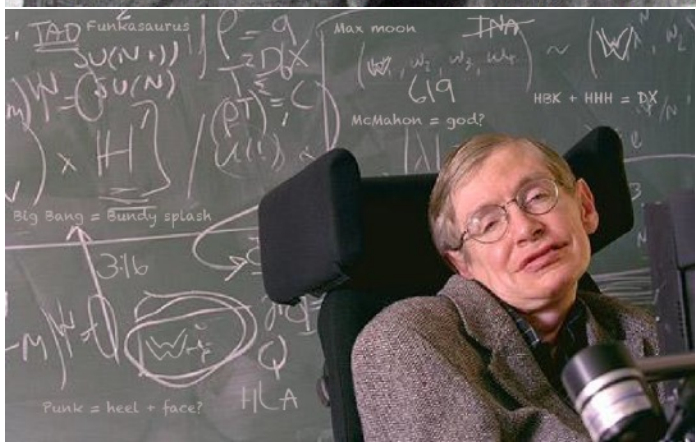
~~*Edsger Dijkstra*~~

- Michael Fellows



Physics





Theoretical physics

- come up with mathematical models

  Nature's language is mathematics

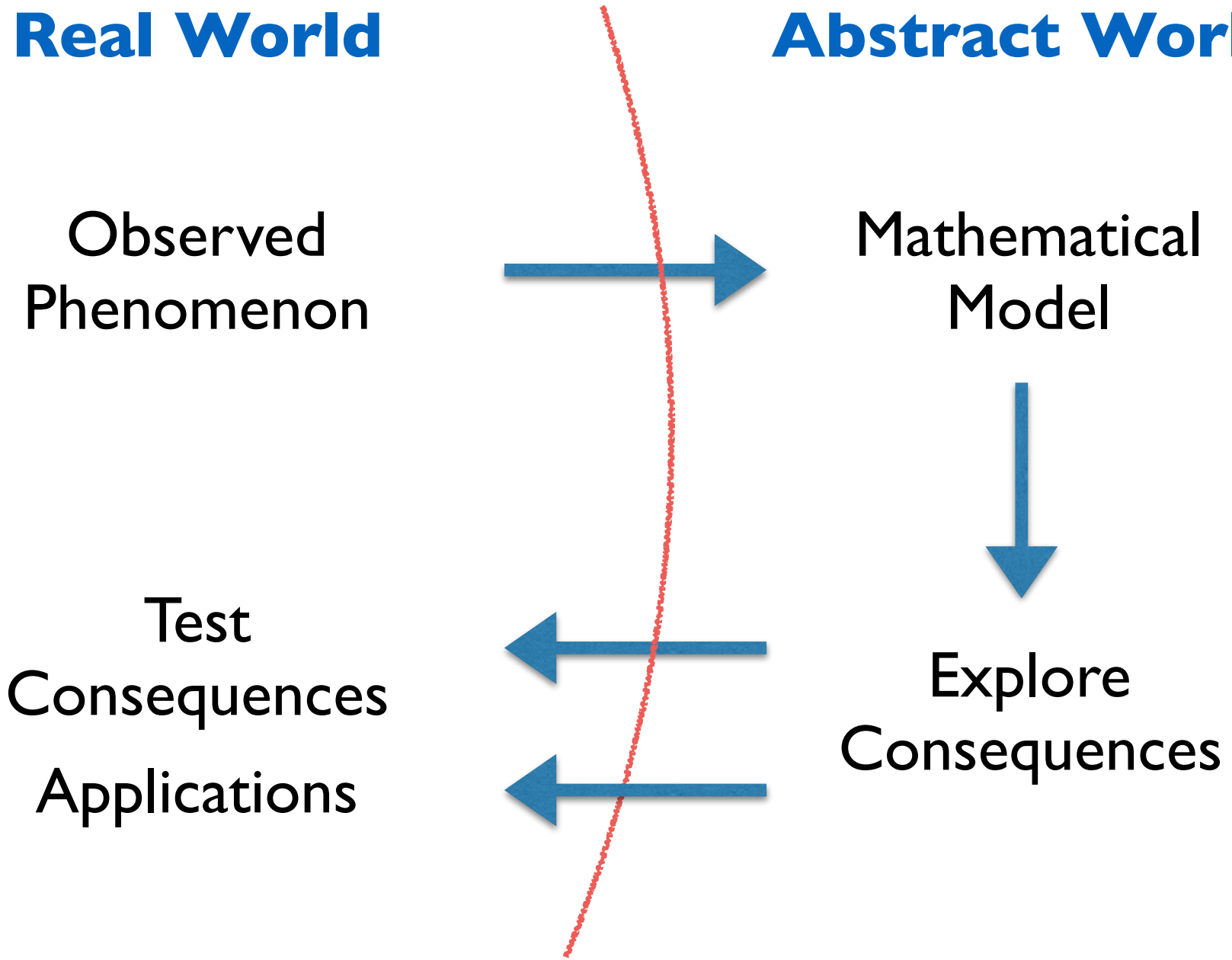
- derive the logical consequences

Experimental physics

- make observations about the universe
- test mathematical models with experiments

Applications/Engineering

The role of theoretical physics



Physics

- science?
- engineering?
- math?
- philosophy?
- sports?

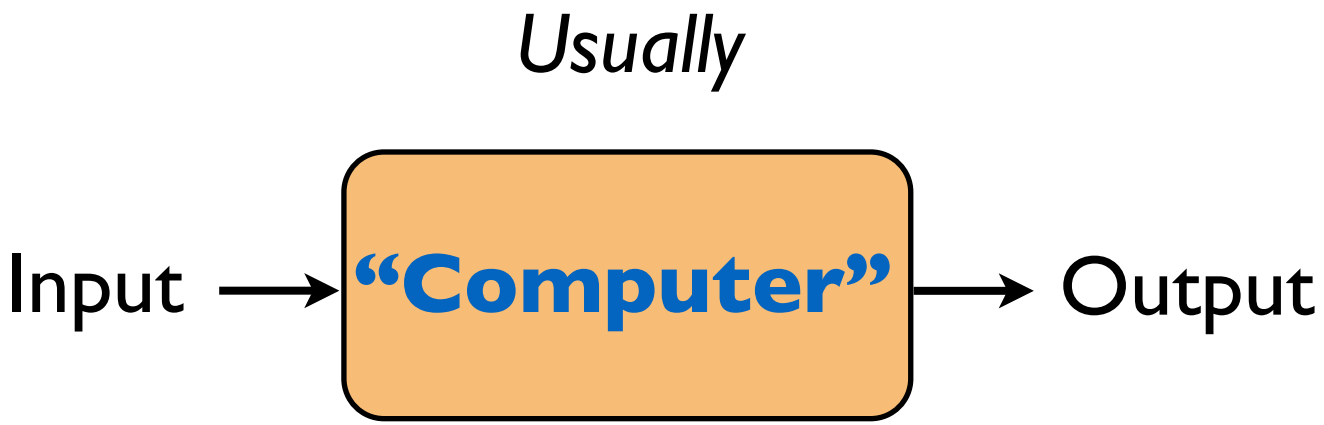
Computer Science

The science that studies computation.

Computation: manipulation of information/data.

Algorithm: description of how the data is manipulated.

Computational problem: the input-output pairs.



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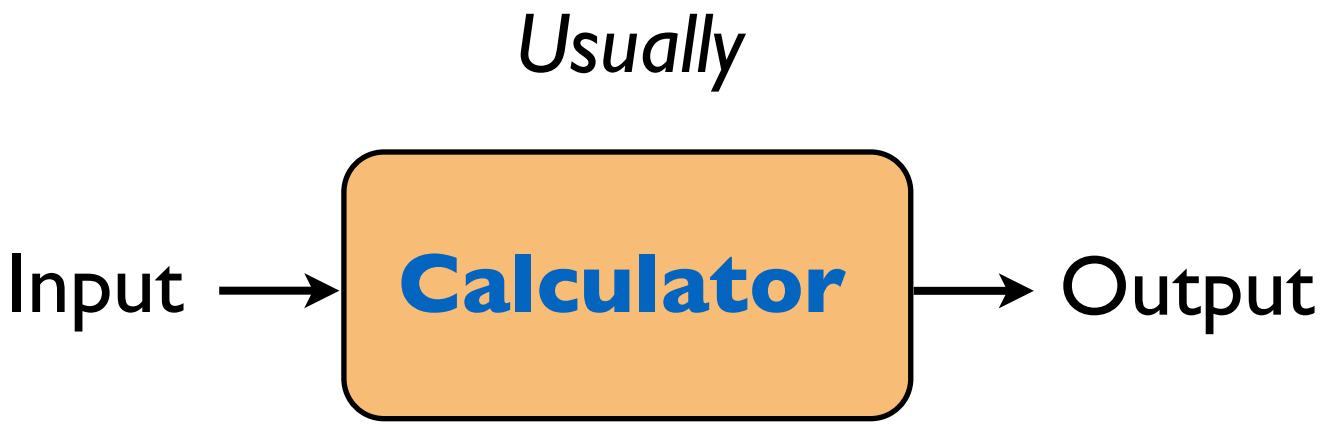

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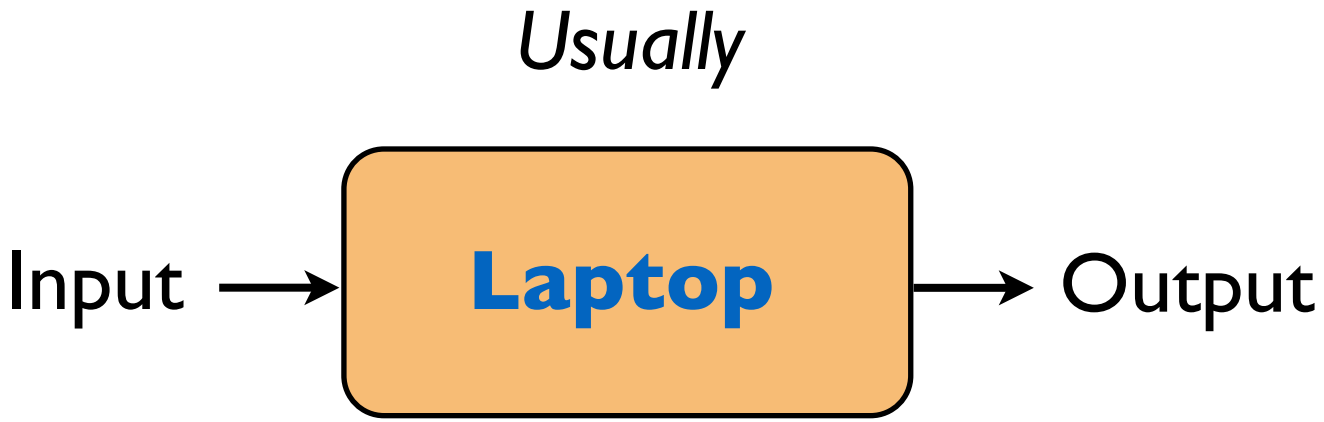

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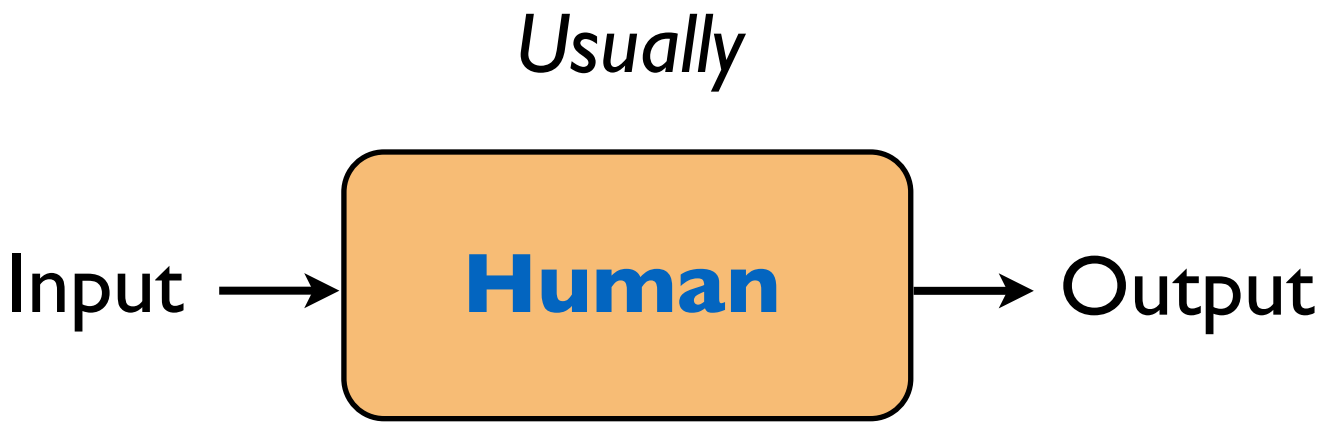

“Computers” in early 20th century

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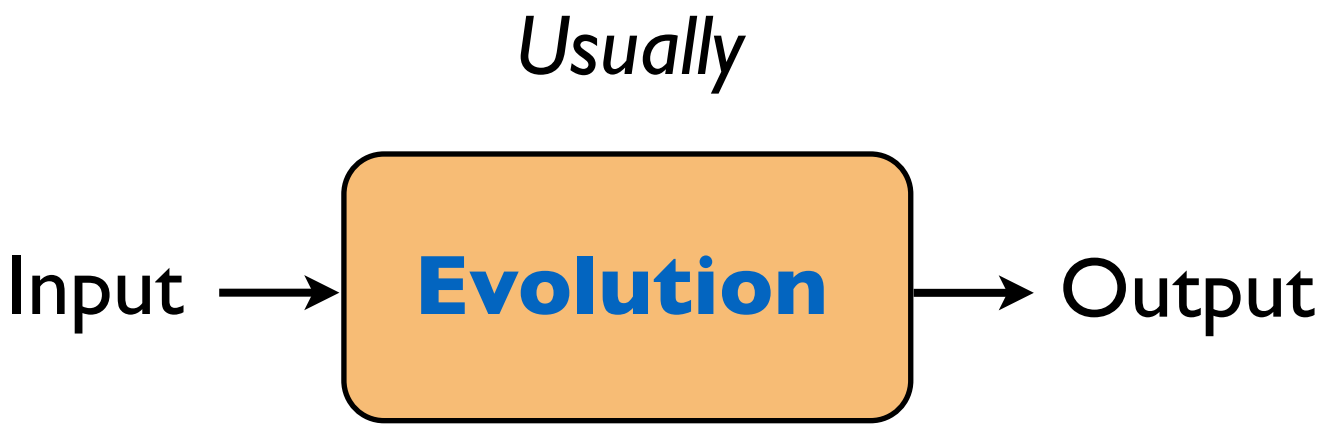


The computational lens

Computational physics

Computational biology

Computational chemistry

Computational neuroscience

Computational economics

Computational finance

Computational linguistics

Computational statistics

Computational social choice

...

The role of theoretical computer science

Build a mathematical model for computation.

Explore the logical consequences.
Gain insight about computation.

http://youtu.be/pTeZP-XfuKI

https://goo.gl/gGkpMv

http://youtu.be/J4TkHuTmHsg

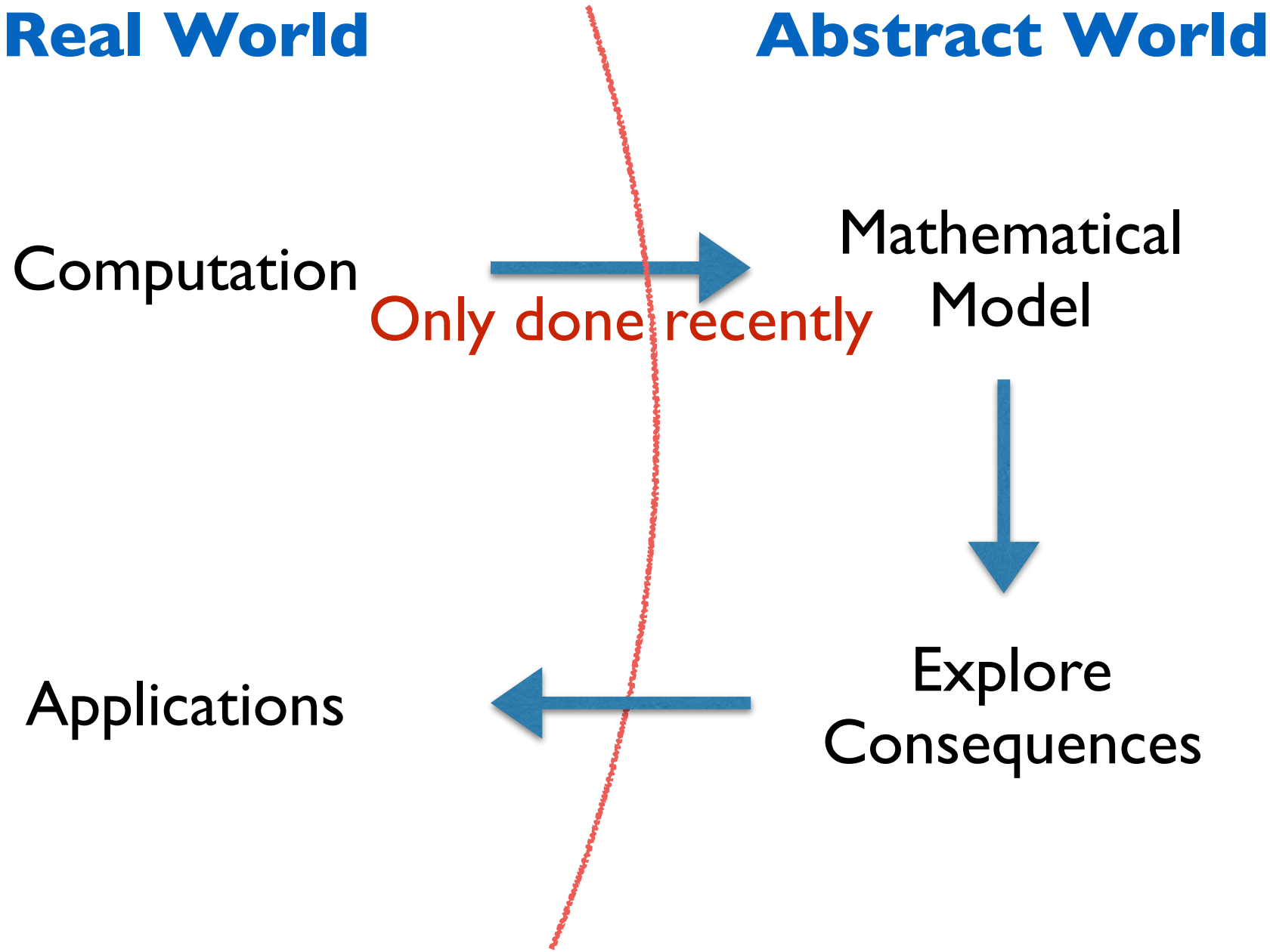
Look for interesting applications.

CMU undergrad

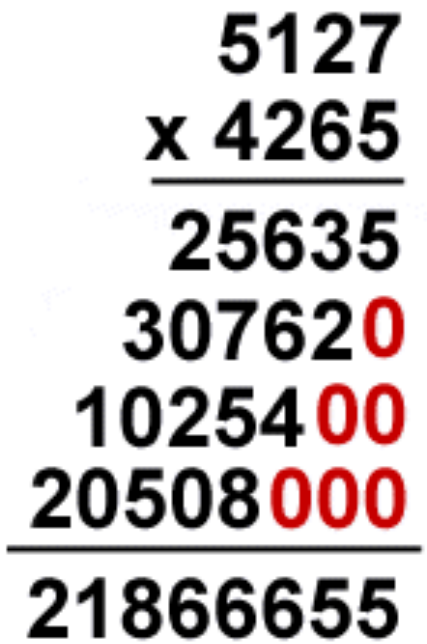
CMU Prof.

OK, we don't have everybody

The role of theoretical computer science



We have been using algorithms for thousands of years.



We have been using algorithms for thousands of years.

Euclid's algorithm (~ 300BC):

```
def gcd(a, b):
    while (a != b):
        if (a > b):
            a = a - b
        else:
            b = b - a
    return a
```

Formalizing computation

Algorithm/Computation was only formalized in the 20th century!

Someone had to ask the right **question**.

David Hilbert, 1900

The Problems of Mathematics

"Who among us would not be happy to lift the veil behind which is hidden the future; to gaze at the coming developments of our science and at the secrets of its development in the centuries to come? What will be the ends toward which the spirit of future generations of mathematicians will tend? What methods, what new facts will the new century reveal in the vast and rich field of mathematical thought?"

2 of Hilbert's Problems

Hilbert's 10th problem (1900)

Is there a finitary procedure to determine if a given multivariate polynomial with integral coefficients has an integral solution?

e.g. $5x^2yz^3 + 2xy + y - 99xyz^4 = 0$

Entscheidungsproblem (1928)

Is there a finitary procedure to determine the validity of a given logical expression?

e.g. $\neg\exists x, y, z, n \in \mathbb{N} : (n \geq 3) \wedge (x^n + y^n = z^n)$

(Mechanization of mathematics)

2 of Hilbert's Problems

Fortunately, the answer turned out to be NO.

2 of Hilbert's Problems

Gödel (1934):

Discusses some ideas for mathematical definitions of computation. But not confident what is a good definition.

Church (1936):

Invents lambda calculus.
Claims it should be the definition of an "algorithm".

Gödel, Post (1936):

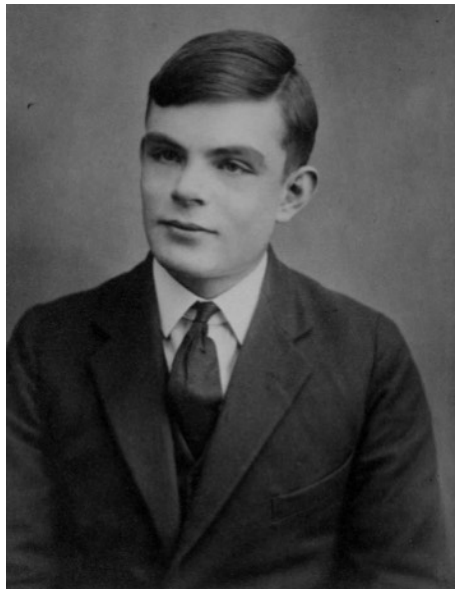
Arguments that Church's claim is not justified.

Meanwhile… in New Jersey… a certain British grad student, unaware of all these debates…

2 of Hilbert's Problems

Alan Turing (1936, age 22):

Describes a new model for computation, now known as the Turing Machine.™



Gödel, Kleene, and even Church:

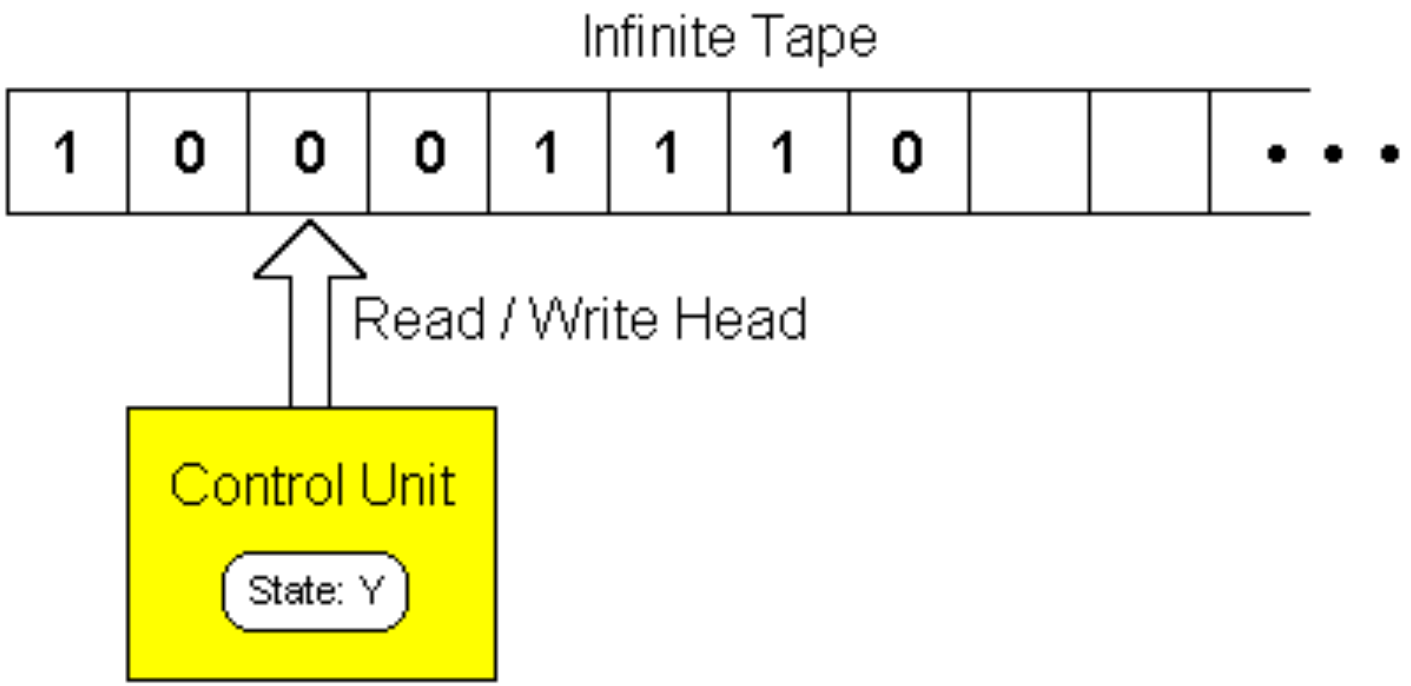
"Umm. Yeah. He nailed it. Game over. 'Algorithm' defined."

Turing (1937):

TMs ≡ lambda calculus

Formalization of computation: Turing Machine

Turing Machine:



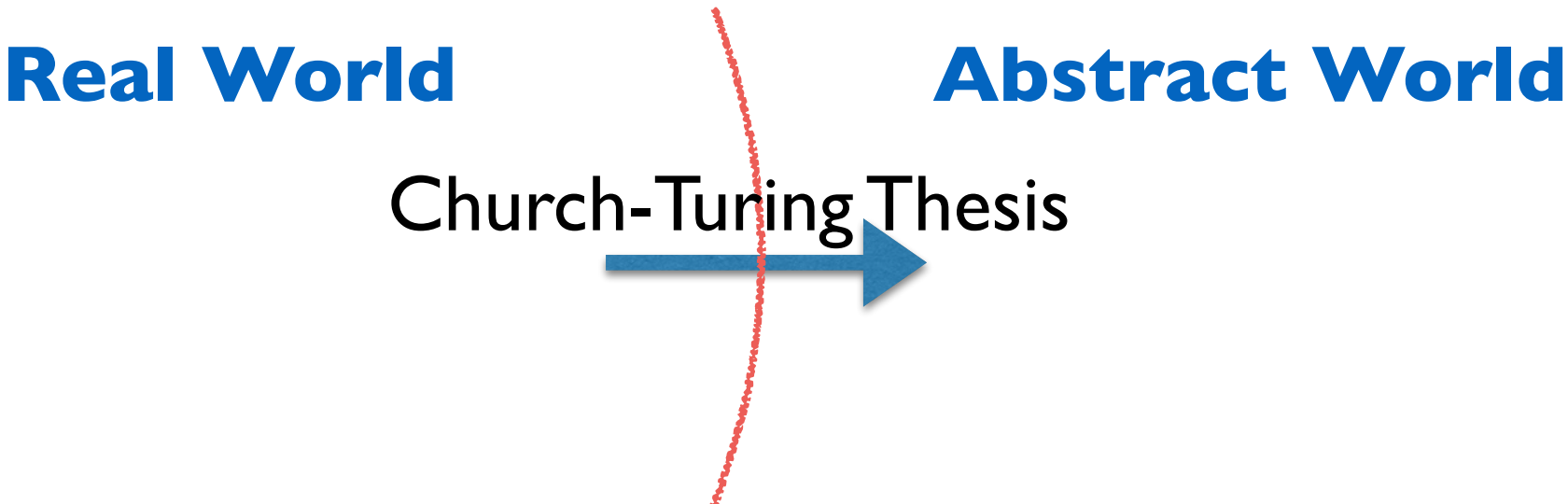
Church-Turing Thesis

Church-Turing Thesis:

The intuitive notion of "computable" is captured by functions computable by a Turing Machine.

(Physical) Church-Turing Thesis

Any computational problem that can be solved by a physical device, can be solved by a Turing Machine.



Back to Hilbert's Problems

Hilbert's 10th problem (1900)

Is there an **algorithm** (a TM) to determine if a given multivariate polynomial with integral coefficients has an integral solution?

e.g. $5x^2yz^3 + 2xy + y - 99xyz^4 = 0$

Entscheidungsproblem (1928)

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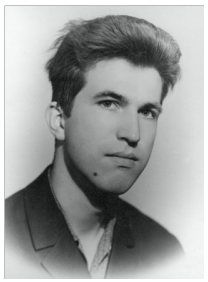
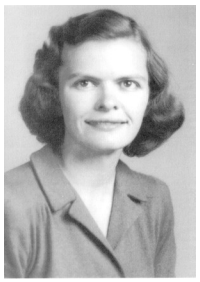
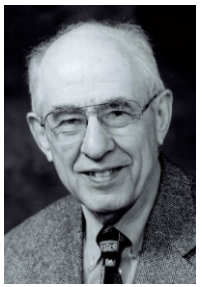
(Mechanization of mathematics)

Back to Hilbert's Problems

Hilbert's 10th problem (1900)

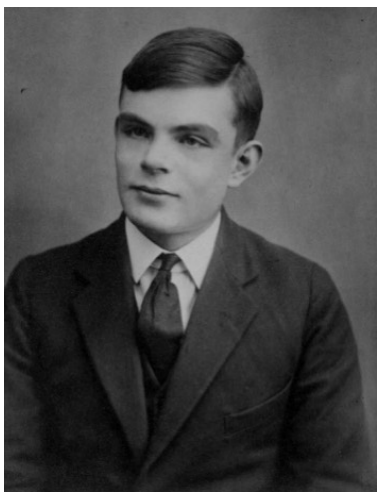
Matiyasevich-Robinson-Davis-Putnam (1970):



There is no algorithm to solve this problem.

Entscheidungsproblem (1928)



Turing (1936):

There is no algorithm to solve this problem.

Computer science

- science?
- engineering?
- math?
- philosophy?
- sports?

More on Theoretical Computer Science (TCS)

2 Main Questions in TCS

Computability of a problem:

Is there an algorithm to solve it?

Complexity of a problem:

Is there an efficient algorithm to solve it?

- time
- space (memory)
- randomness
- quantum resources

Computational Complexity

Complexity of a problem:

Is there an efficient algorithm to solve it?

- time
- space (memory)
- randomness
- quantum resources

2 camps:

- trying to come up with efficient algorithms (algorithm designers)
- trying to show no efficient algorithm exists (complexity theorists)

Computational Complexity

2 camps:

- trying to come up with efficient algorithms (algorithm designers)
- trying to show no efficient algorithm exists (complexity theorists)

multiplying two integers

factoring integers

detecting communities in social networks

protein structure prediction

simulation of quantum systems

computing Nash Equilibria of games

Some other interesting questions

P vs **NP**

Some other interesting questions

Time vs **Space**

Some other interesting questions

Deterministic vs **Randomized**

Some other interesting questions

Cryptography and **Security**

Some other interesting questions

Socioeconomics

(e.g. privacy, fairness)

Some other interesting questions

Learning Theory

Some other interesting questions

Quantum Computation

Some other interesting questions

...

Learning Objectives

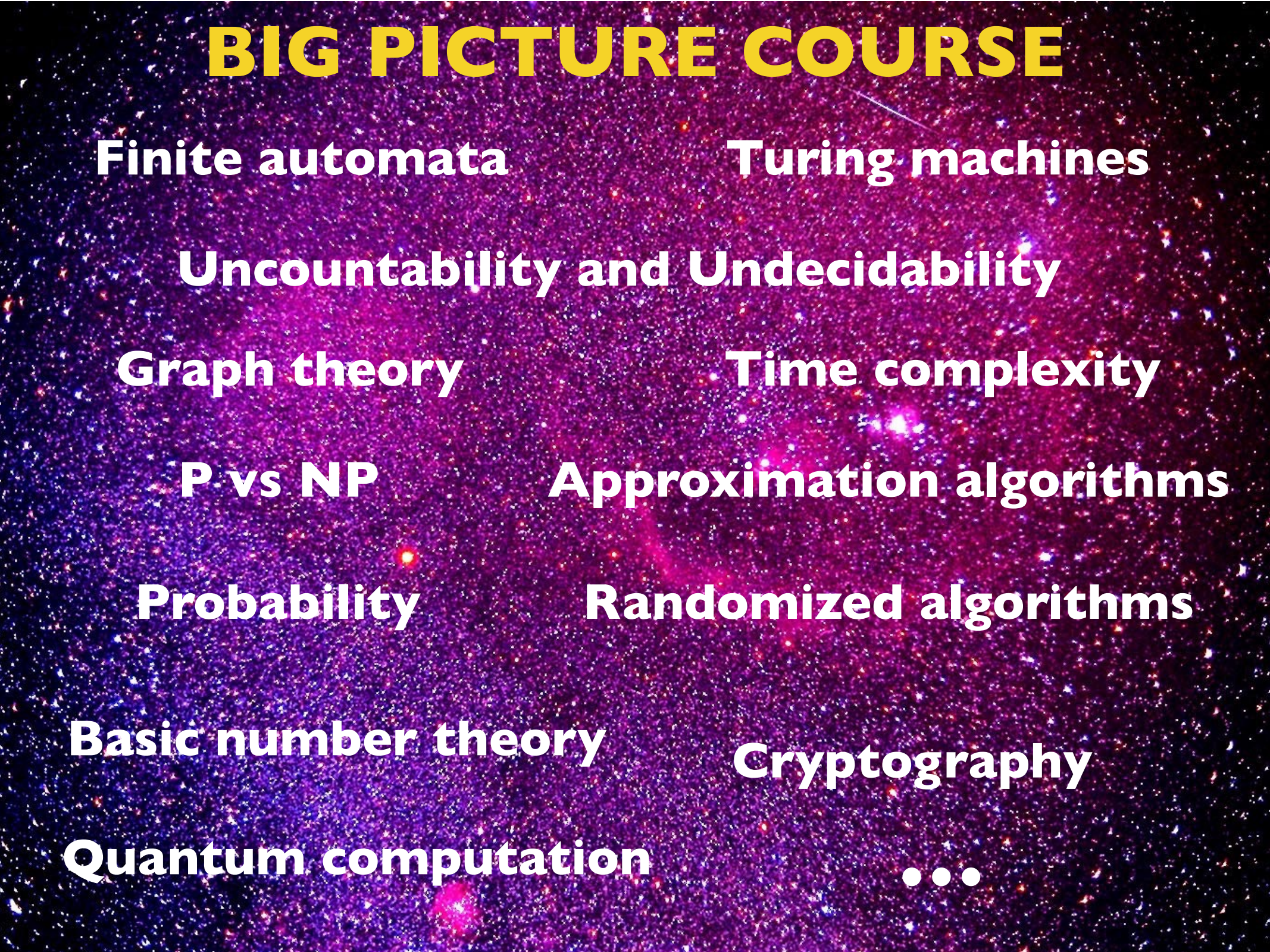
Perspective I

Overview of Topics

Part I: Formalizing the notions of
problems, algorithms, and computability.

Part 2: Computational complexity:
theory and applications.

Part 3: Randomness in CS and
some highlights of theoretical CS.


BIG PICTURE COURSE
Finite automata
Turing machines
Uncountability and Undecidability
Graph theory
Time complexity
P vs NP
Approximation algorithms
Probability
Randomized algorithms
Basic number theory
Cryptography
Quantum computation
...

Perspective I

Goals

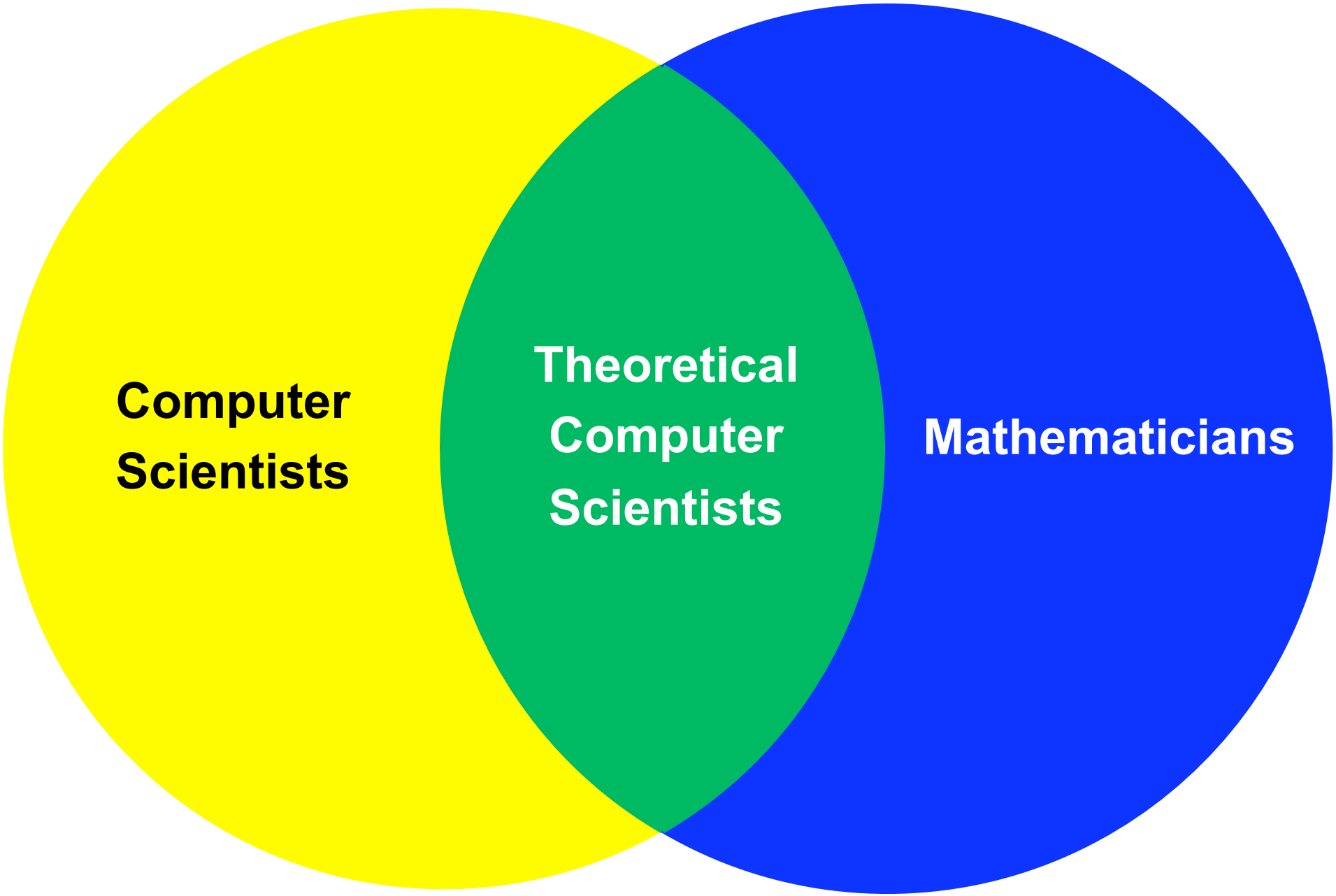
- Provide a formal introduction to the foundations of computer science.

- Improve your rigorous, logical and abstract thinking skills.

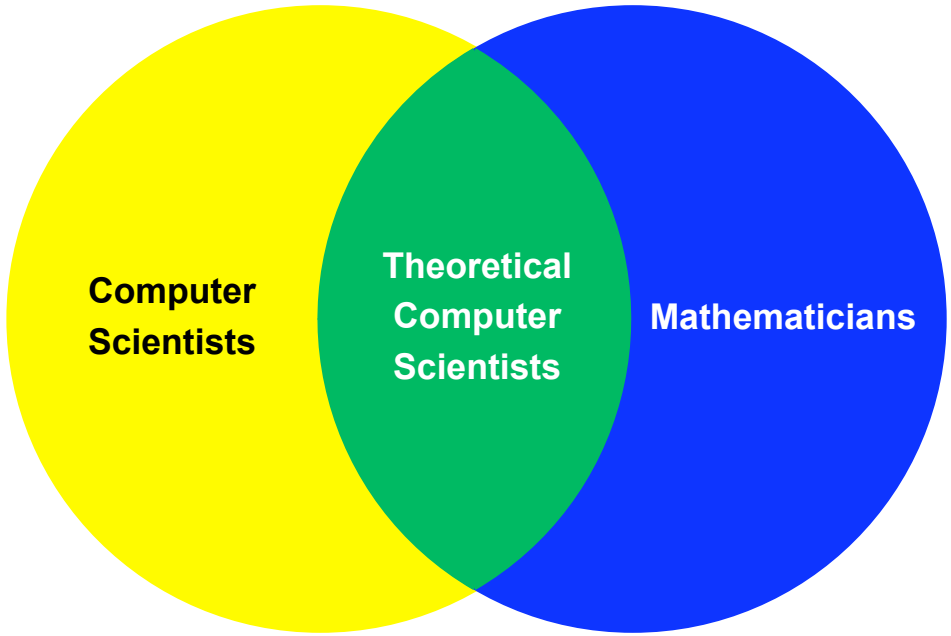
- Prepare you to be innovators in computer science.

- Push you to strive for clarity of thought and clarity in expression of thought.

Perspective 2



Perspective 2



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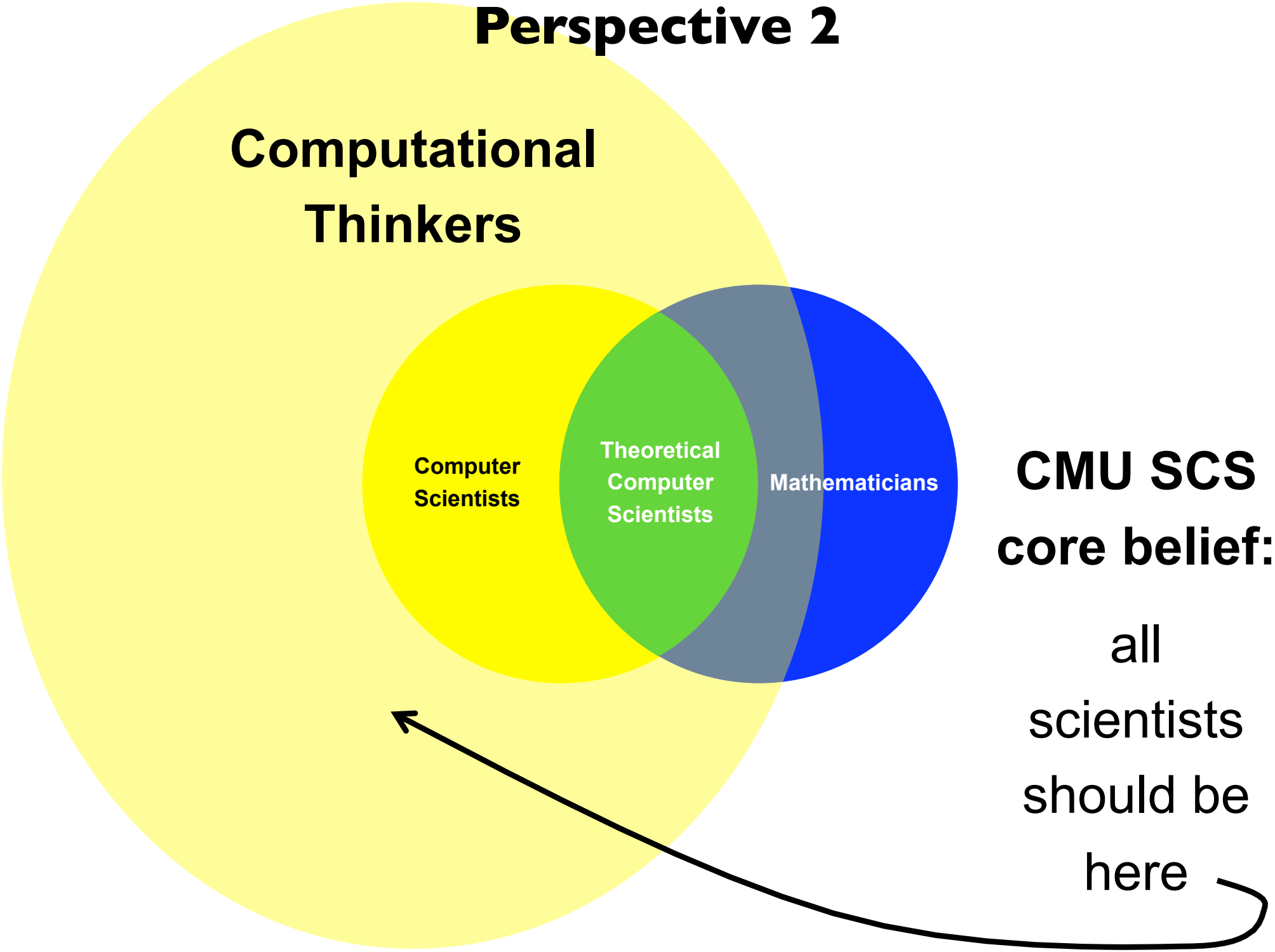
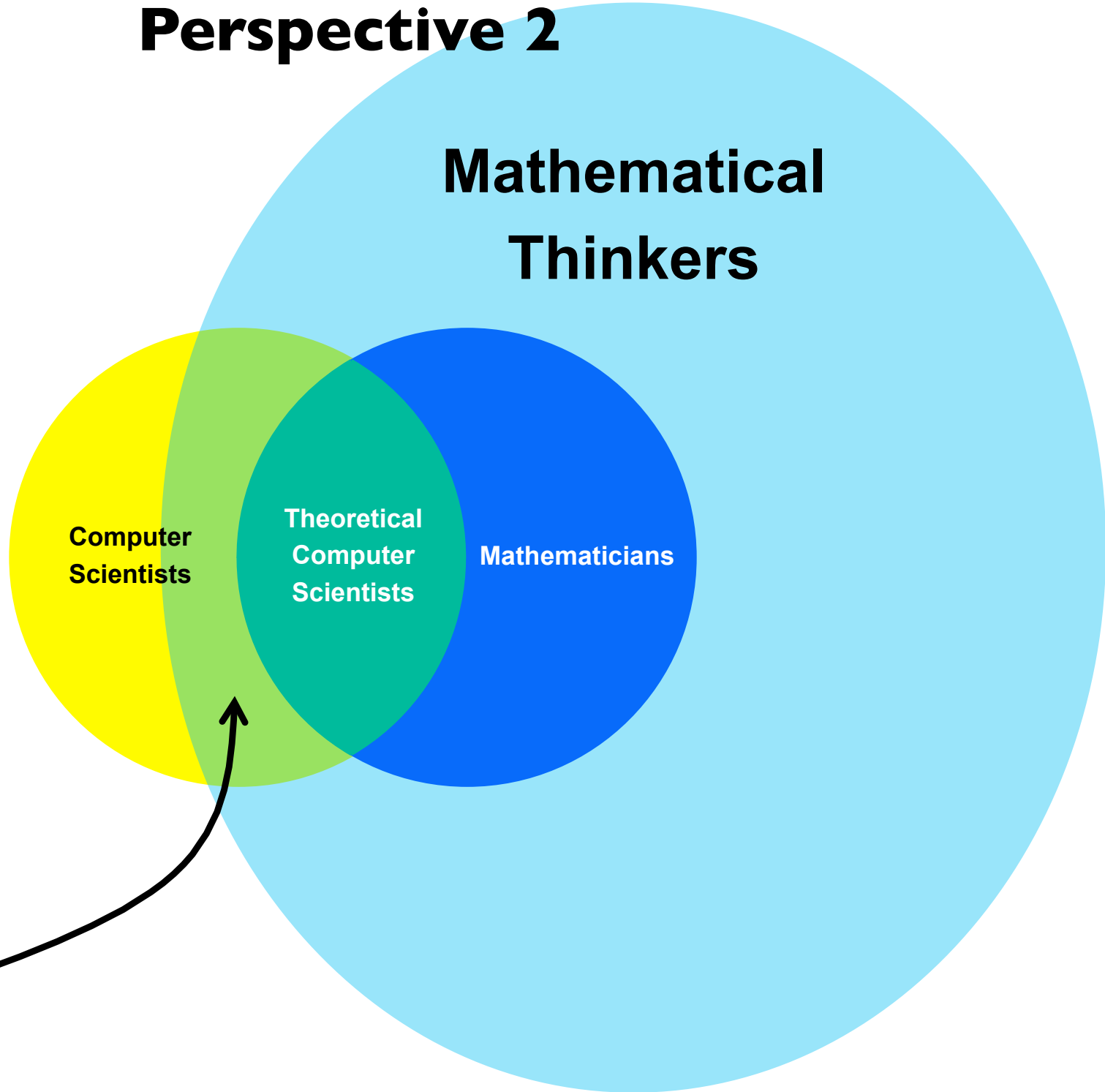


CMU SCS core belief:

all scientists should be here

Perspective 2



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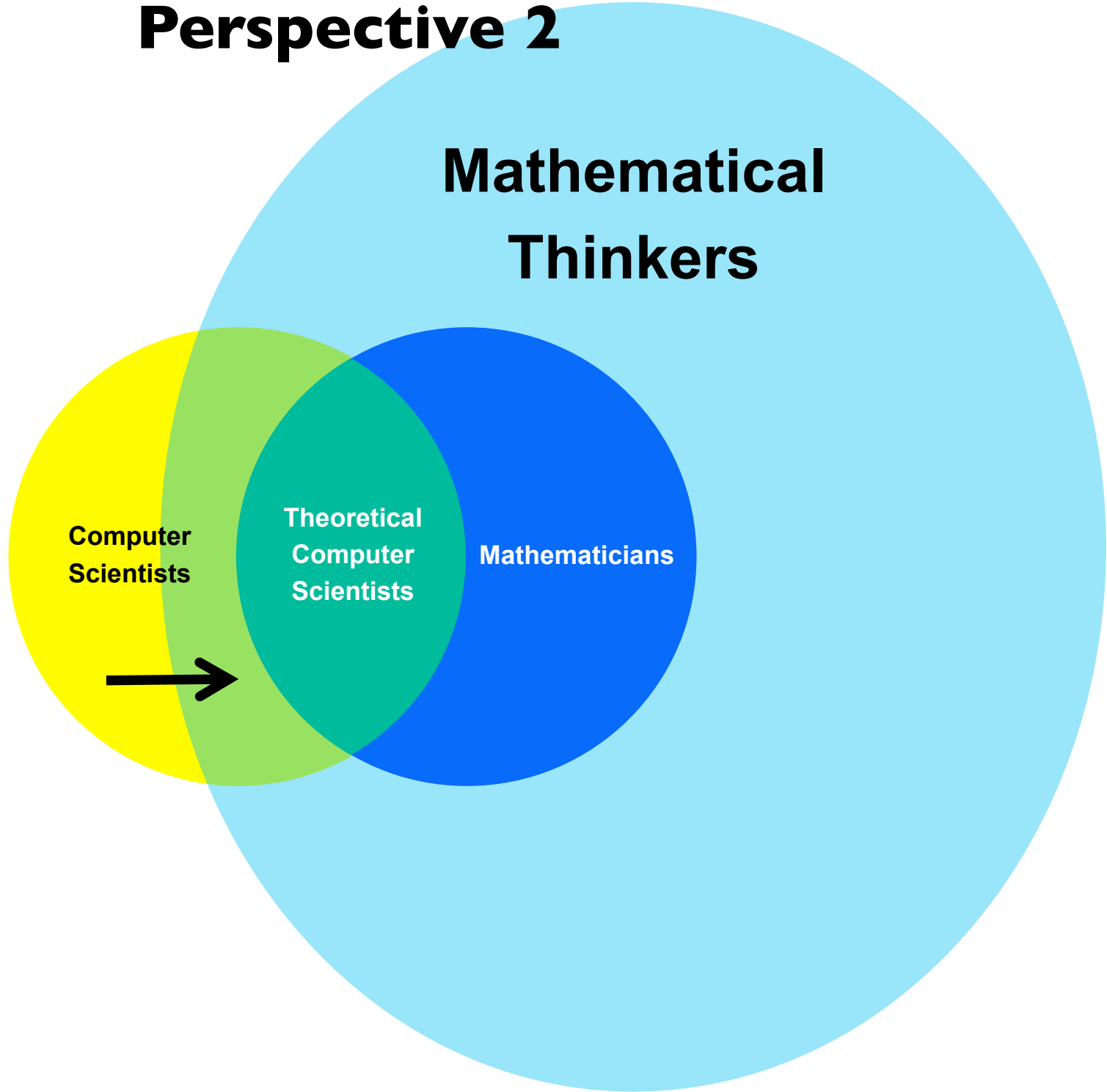
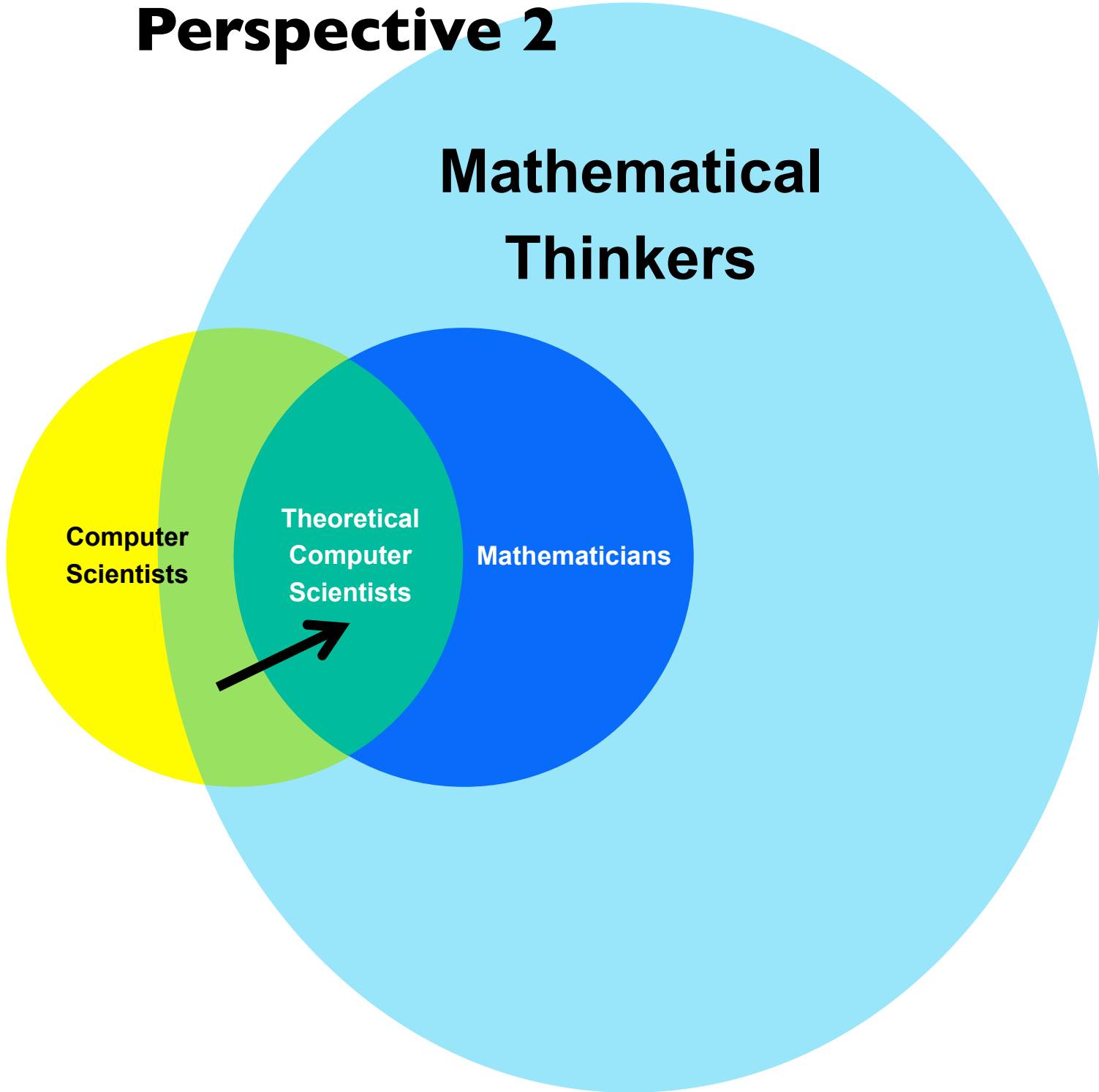


Goal #1 of 15-251

Perspective 2



Goal #2 of 15-251 (maybe)

Perspective 3

Mathematics is like… cilantro.

There are **5** kinds of people when it comes to cilantro.

Perspective 3

1. People who do not know what cilantro is.

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Perspective 3

1. People who do not know what cilantro is.

 Coriandrum sativum

 Coriander (leaves)

 香菜

 धनिया

 고수

 زیـنشگ

 الكزبرة

 ngò

 φύλλα κόλιανδρου

 கொத்தமல்லி

 ধনে

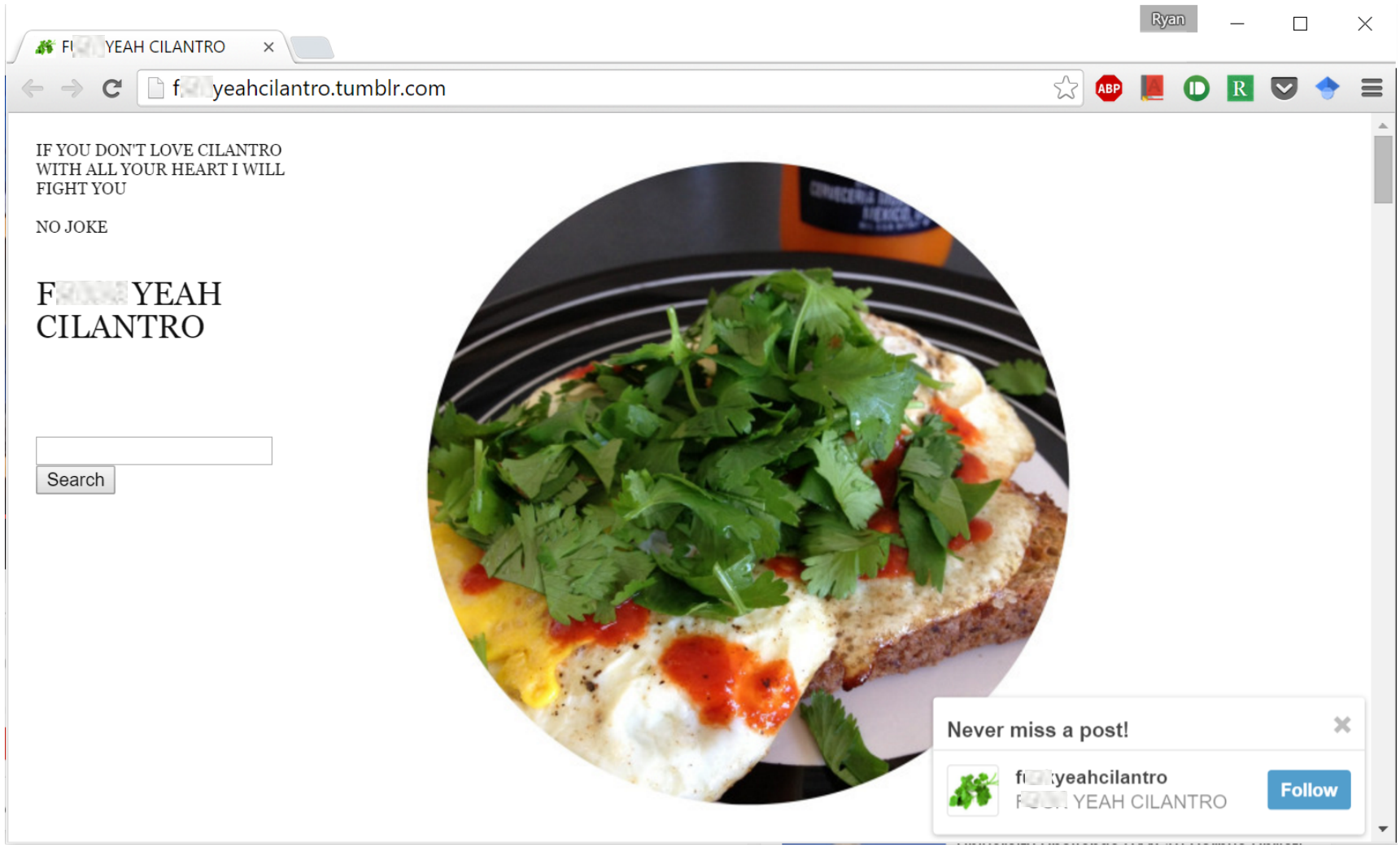
 kişniş

 кинза

 כוסברה

Perspective 3

2. People who love cilantro.



Perspective 3

3. People who think cilantro is fine.

Goal: have everyone at least in this category by the end of the course.

Perspective 3

4. People who don't like cilantro.

Still gotta try it.

Hope to move you to previous category.

If not, hope you can eat cilantro if necessary.

Perspective 3

5. People with a genetic condition that makes cilantro taste like soap.

Is this true?

Video

Course webpage: www.cs.cmu.edu/~15251

Lecture tomorrow: DH 2210 6:30 - 7:50pm